



Brookhill
Institute of Mathematics

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Using Depth of Knowledge to Add
Rigor to the Mathematics Classroom

Wisconsin Mathematics Council
Annual Conference
May 5, 2016

Vision Statement



The Brookhill Institute of Mathematics exists to raise the mathematical literacy of every learner.

Introductions

Who we are:

- Paige Richards
- Jeff Ziegler

Who are you?

Learning Intentions & Success Criteria

We are building a common language around rigor.

We will be successful when we can define and begin to quantify mathematical rigor using Webb's Depth of Knowledge.

What does **rigor**
look like in mathematics
classrooms?



Why is Rigor Important?

“Student learning is greatest in classrooms where the tasks consistently encourage high-level student thinking and reasoning and least in classrooms where the tasks are routinely procedural in nature.”

Principles to Actions: Ensuring mathematical success for all (NCTM, 2014)



“The Common Core State Standards require **high-level cognitive demand**, such as asking students to demonstrate deeper conceptual understanding through the application of content knowledge and skills to new situations and sustained tasks.”

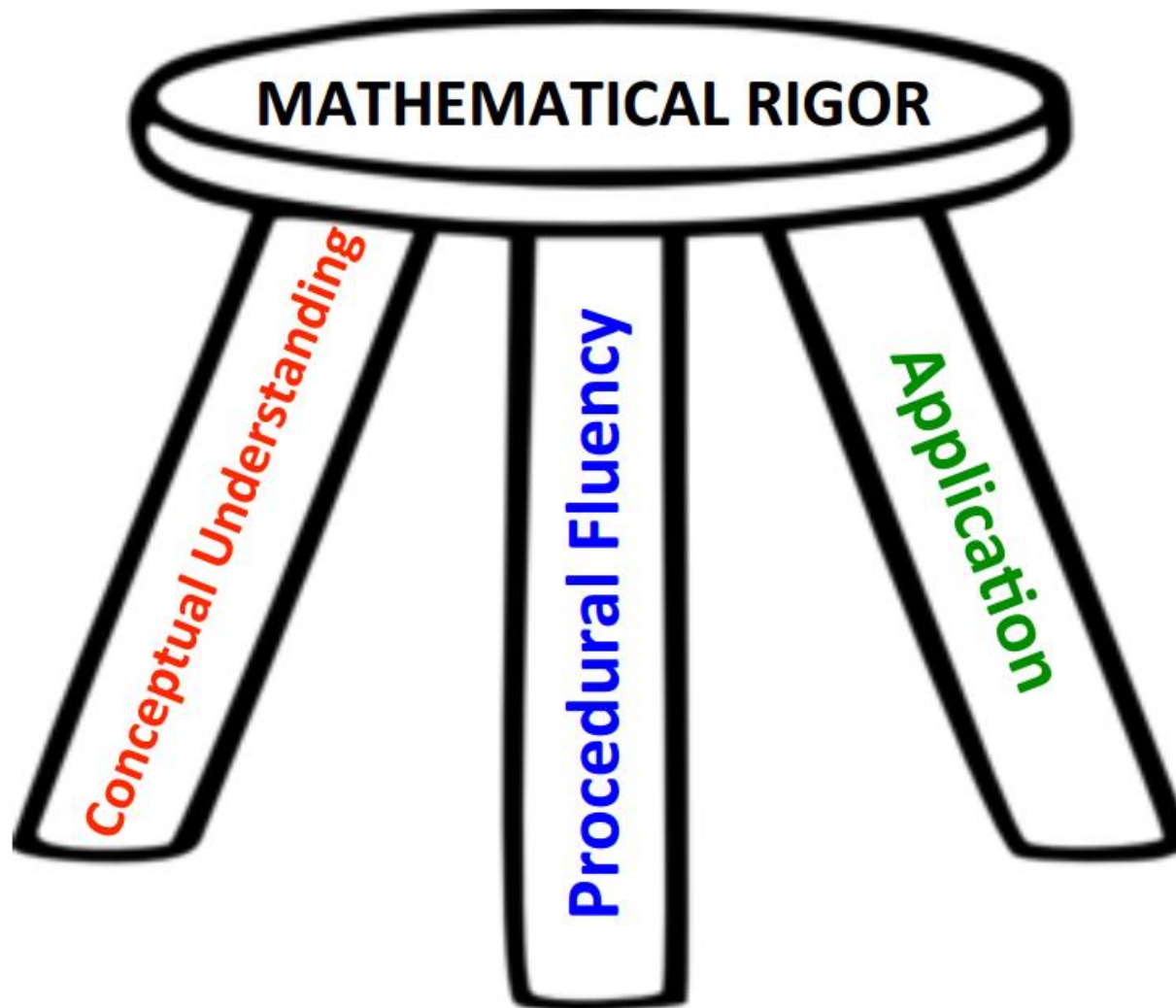
*Smarter Balanced Mathematics
Item Specifications Appendix B*



From WI DPI



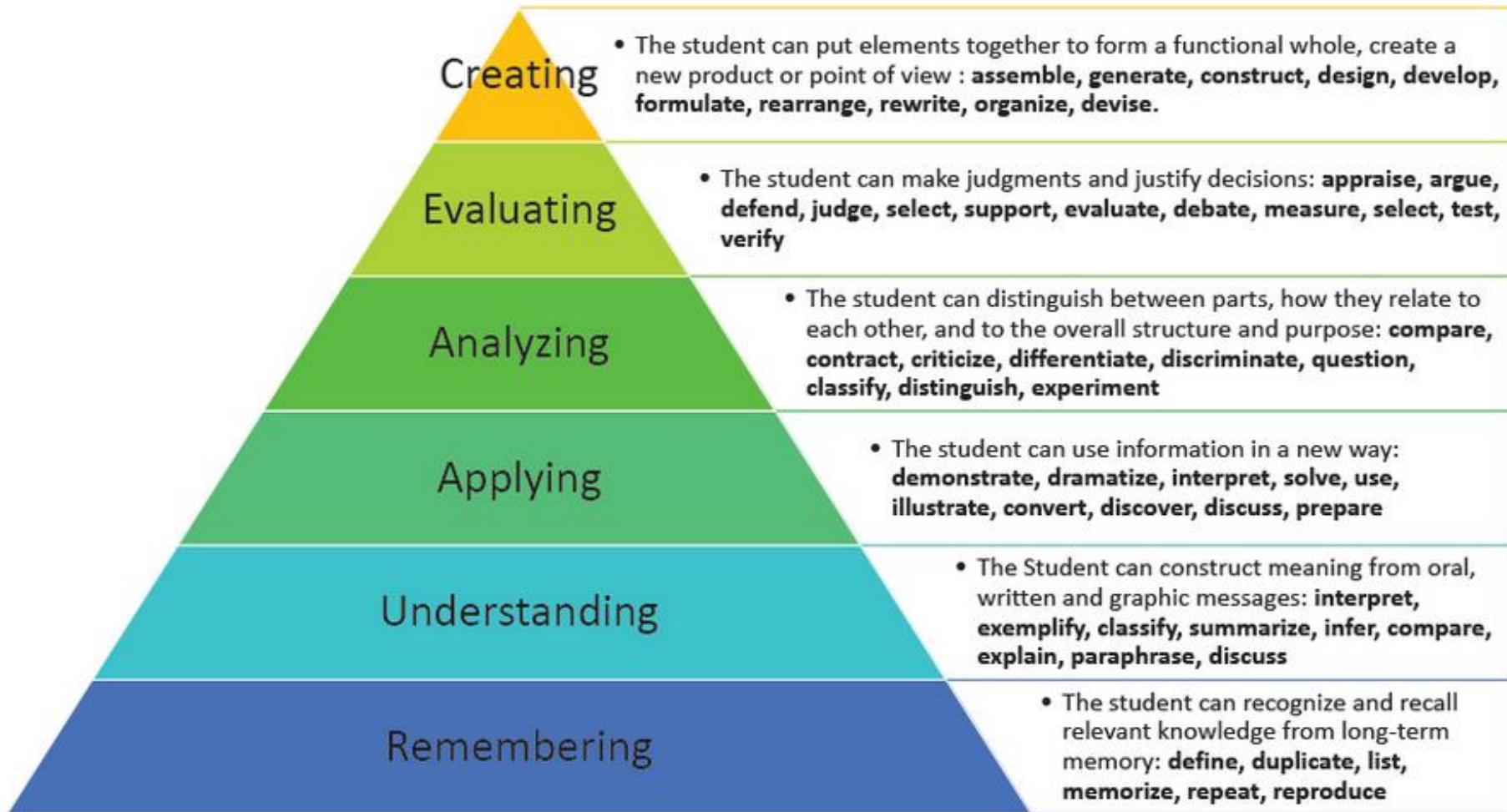
- Focus
- Coherence
- Rigor



MATHEMATICAL RIGOR - It's for ALL students

Building a Common Language

Bloom's Revised Taxonomy



DOK Wheel



Webb's Depth of Knowledge (DOK)

DOK categorizes tasks according to the complexity of thinking required to successfully complete them.

DOK Level 1:

Recall

DOK Level 2:

Skills/Concept

DOK Level 3:

Strategic Thinking

DOK Level 4:

Extended Thinking

Depth of Knowledge

Level 1: Recall – Recall of a fact, information or procedure.

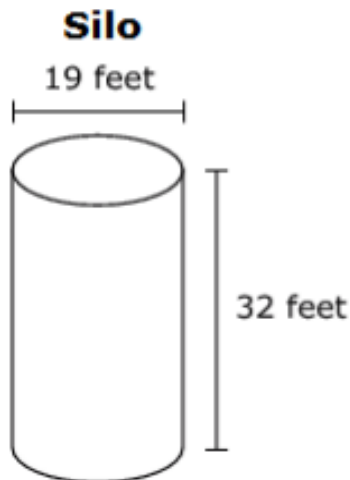
Level 2: Skills/Concept – Use information or conceptual knowledge, two or more steps, etc.

Level 3: Strategic Thinking – Requires reasoning, developing a plan or sequence of steps, some complexity, or non-routine, more than one possible answer.

Level 4: Extended Thinking – Requires an investigation, time to think and process multiple conditions of the problem.

Webb, 2015

An empty corn silo in the shape of a cylinder is being filled with corn.



The silo is filled at a constant rate for a total of 10 hours. The table shows the amount of corn, in cubic feet, in the silo at the given number of hours after filling started.

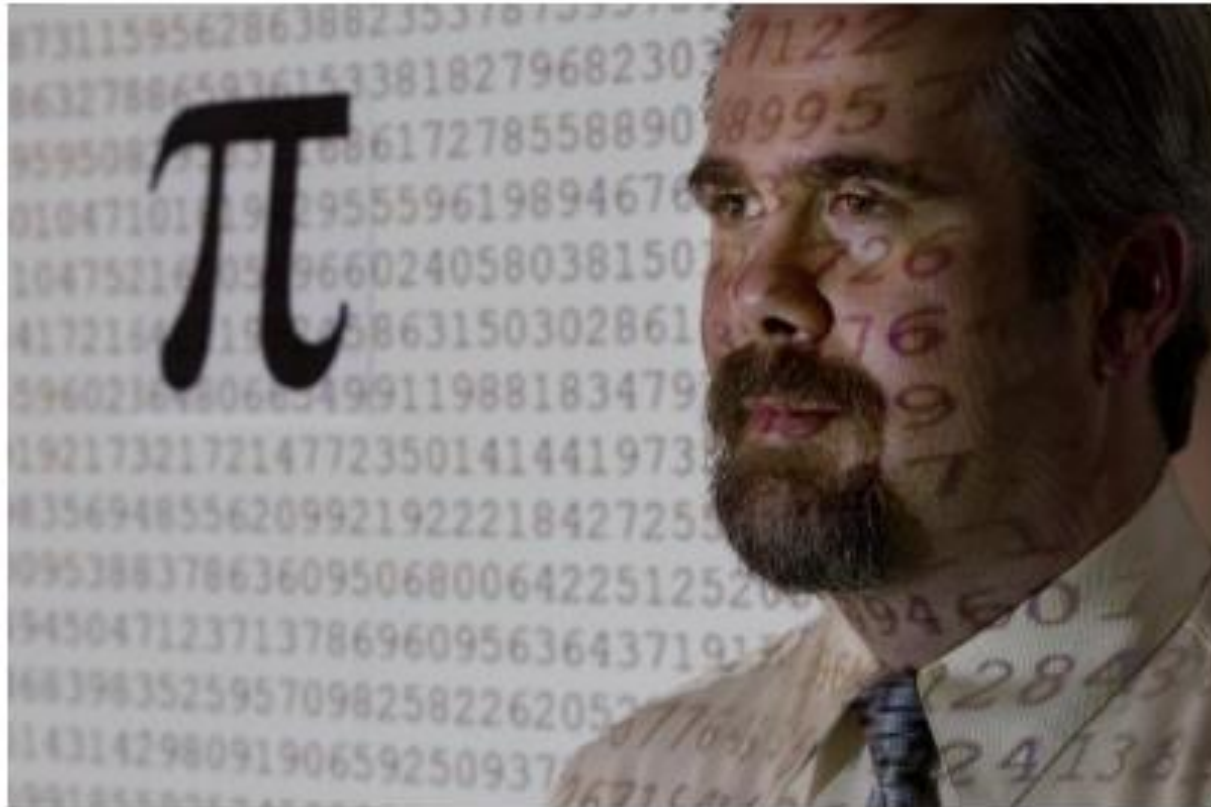
Number of Hours	Amount of Corn (cu ft)
0	0
3	2475
5	4125
8	6600

Enter the **percent** of the silo that is filled with corn at 10 hours.

Decide if each equation is true or false. Click True or False for each equation.

	True	False
$3 \times 6 = 18 \div 2$	<input type="checkbox"/>	<input type="checkbox"/>
$4 \times 9 = 36 \div 4$	<input type="checkbox"/>	<input type="checkbox"/>
$2 \times 5 = 20 \div 2$	<input type="checkbox"/>	<input type="checkbox"/>

Difficult but not complex! Still a Level 1



MATT ROURKE/AS SOCIATED PRESS

Marc Umile has recited pi to 12,887 digits.

<http://www.nydailynews.com/news/national/geek-best-ways-celebrate-pi-day-article-1.1287969here>

3rd Grade Standards

Operations and Algebraic Thinking (3.OA)

Represent and solve problems involving multiplication and division.

4. Determine the unknown whole number in a multiplication or division equation relating three whole numbers. *For example, determine the unknown number that makes the equation true in each of the equations $8 \times ? = 48$, $5 = ? \div 3$, $6 \times 6 = ?$.*

3rd Grade Standards

Operations and Algebraic Thinking (3.OA)

Understand properties of multiplication and the relationship between multiplication and division.

5. Apply properties of operations as strategies to multiply and divide.² *Examples: If $6 \times 4 = 24$ is known, then $4 \times 6 = 24$ is also known. (Commutative property of multiplication.) $3 \times 5 \times 2$ can be found by $3 \times 5 = 15$, then $15 \times 2 = 30$, or by $5 \times 2 = 10$, then $3 \times 10 = 30$. (Associative property of multiplication.) Knowing that $8 \times 5 = 40$ and $8 \times 2 = 16$, one can find 8×7 as $(8 \times 5) + (8 \times 2) = 40 + 16 = 56$. (Distributive property.)*

²Students need not use formal terms for these properties.

Mathematics DOK Definitions

Individually:

- Read DOK definitions

With a partner:

- Compare Level 1 & Level 2
- Compare Level 2 & Level 3
- Use evidence from the definitions in your discussion

Examining Standards & Objectives for DOK

Before we look at math tasks,
we must consider the
standards we are teaching
and later assessing.



Digging into Standards

With a partner:

- Read the sample mathematics objectives.
- Determine DOK of each objective.
- Use **evidence** from the definitions.
- Compare your Levels to Webb and Associates

Examining Sample Mathematics Assessment Items for DOK

If our instruction is designed around standards at different DOK Levels, then we should assess student learning at different DOK Levels.

Digging into Assessment Items

With a partner:

- Read sample assessment items 5, 6, 9.
- Determine DOK of each item.
- Use evidence from the definitions.
- If you have time discuss additional assessment items.

Digging into Assessment Items

With a partner:

- Compare your levels to Webb and Associates.
- Discuss any differences.
- Revisit definitions.

What does this mean for
my practice?

Tips from Webb

1. Clarify important learning outcomes and priorities.
2. Plan and deliver effective instruction.
3. Select and design appropriate assessments.
4. Align standards, instruction, and assessments.

Webb, 2015

Assigning DOK Levels

Key Considerations

- Collaboration is key
- Student experience matters
- DOK is not about verbs
- Difficult is not the same as complex
- Context does not guarantee rigor
- Align standards, instruction, assessment

Big Ideas of DOK

- Levels are continuous **NOT** discrete
- DOK is **NOT** a progression
- Level numbers are **NOT** a value judgment
- **ALL** levels are important for **ALL** students
- Implementation is critical
- Definitions are specific to each discipline

Reflections

As you think about going back to your district, in what ways will you support teachers to assure that student assessments reflect the depth of knowledge of the standards?

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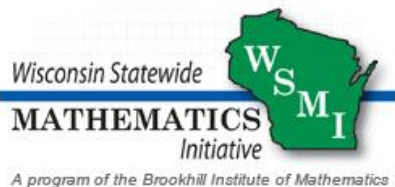
MISSION STATEMENT

Our mission is to provide K-12 teachers and higher education the opportunity to participate, collaborate, develop, and improve the teaching of mathematics.

UPCOMING EVENTS

Jan 11, 2016
DPI H.S. Work Group

www.wsmi.net



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Establish a sustainable, statewide effort for high quality mathematics education and learning!

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Organization/School/District *

Sign Up

Module Content

- K-2: Operations and Algebraic Thinking
- K-2: Number and Operations in Base Ten
- 3-5: Operations and Algebraic Thinking
- 3-5: Number and Operations Fractions
- 6-8: Ratios and Proportional Relationships
- 6-8: Expressions and Equations
- 6-8: Statistics
- 9-12: Statistics and Probability for ALL High School Mathematics Teachers
- 8-12: Algebra and Functions with Modeling

WSMI Institutes

K-2 Operations and Algebraic Thinking
and
3-5 Operations and Algebraic Thinking
are CLOSED at Greendale and
Sauk Prairie!

3-5 Operations and Algebraic Thinking
And
6-8 Expressions and Equations
are CLOSED at New London!

Summer 2016

CESA 3 June 20-24

West Salem July 11-15
New London

Sauk Prairie July 18-22

DC Everest August 1-5
Greendale

Thank you!

Mathematics Program Specialists

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